CONTROLLER TUNING FOR INDUSTRIAL PROCESS-A SOFT COMPUTING APPROACH

B.Nagaraj, P.Vijayakumar

Corresponding author, Karunya University, Coimbatore, India
email:nagarajice@gmail.com
Karapagam College of Engineering, Coimbatore, India

Abstract

Proportional – Integral – Derivative control schemes continue to provide the simplest and effective solutions to most of the control engineering applications today. However PID controller is poorly tuned in practice with most of the tuning done manually which is difficult and time consuming. This research comes up with a soft computing approach involving Genetic Algorithm, Evolutionary Programming, Particle Swarm Optimization and Bacterial foraging optimization. The proposed algorithm is used to tune the PI parameters and its performance has been compared with the conventional methods like Ziegler Nichols and Cohen Coon method. The results obtained reflect that use of heuristic algorithm based controller improves the performance of process in terms of time domain specifications, set point tracking and regulatory changes and also provides an optimum stability. This paper discusses in detail, the Soft computing technique and its implementation in PI tuning for a controller of a real time process. Compared to other conventional PI tuning methods, the result shows that better performance can be achieved with the soft computing based tuning method. The ability of the designed controller in terms, of tracking set point is also compared and simulation results are shown.

Keywords: Bacterial foraging, Genetic algorithm, Particle swarm optimization, PID controller
1 Introduction

PID controller is a generic control loop feedback mechanism widely used in industrial control systems [1]. It calculates an error value as the difference between measured process variable and a desired set point [2]. The PID controller calculation involves three separate parameters proportional, integral and derivative values. The goal of PID controller tuning is to determine parameters that meet closed loop system performance specifications and the robust performance of the control loop over a wide range of operating conditions should also be ensured. Practically, it is often difficult to simultaneously achieve all of these desirable qualities [3]. The purpose of this paper is to investigate an optimal controller design for a simple process in Paper machine using the evolutionary Programming, Genetic Algorithm, Particle Swarm Optimization and Bacterial foraging Optimization.

Objective of the research is to develop a soft computing based PID tuning methodology for optimizing the control of a simple Process plant that is housed in the Paper Machine#3 at the Tamilnadu Newsprint and Papers Limited, India. The main variables under control are chemical flow, Pump discharge pressure and tank level. This research proposes the development of a tuning technique that would be best suitable for optimizing the processes operating in a single-input-single-output (SISO) process control loop. The SISO topology has been selected for this study because it is the most fundamental of control loops and the theory developed for this type of loop can be easily extended to more complex loops [4]. The efficacy of the proposed method has been proved to be the best by comparing the control performance of loops with the soft computing method to that of loops tuned using the conventional method of Ziegler-Nichols method.

2 Development of a Mathematical model of Real Time Process

The plant used for this study is given in appendix (fig.9) and its corresponding P & ID schematic is shown in Fig 1. The plant consists of a storage tank: Process tank feed chemical pump, Control Valve and Pressure level and flow transmitters. A feed-pump supplies chemical from the storage tank to the process tank. The Pressure transmitter (PT 0.01A), which is situated downstream of the pump, provides an indication of pump discharge pressure and volume of water moved by
the pump. Control valve (CV 0.01A) is situated between the flow transmitter and the process tank to manipulate the flow and thus control the discharge pressure and the level of water in the process tank. Control of the water flow rate (FT 0.01A), line pressure (PT 0.01A) and process tank level (LT0.01A) is achieved separately using the control valve (CV 0.01A) during each control session. A current to pressure (I/P) converter is used to provide correct signal interface to the control valve (CV 0.01A), which operates from a 4 bar air supply.

![Diagram](image)

**Fig.1.** P&ID of the plant under study.

### 2.1 Identification of Process Parameters

The Process model used in the experiments for the pressure, flow and level control loops are given in (1), (2) and (3) respectively. Models (1)-(3) were identified with
Matlab system identification tool box[5] and used to determine the tuning parameters by means of the ZN, GA, EP, PSO and BFO tuning methodologies.

Pressure Control System:

\[ GP_{\text{pressure}}(s) = \frac{0.62 \exp(-0.15s)}{(0.5s+1)} \] \hspace{1cm} (1)

Flow Control System:

\[ GP_{\text{flow}}(s) = \frac{0.5 \exp(-6.5s)}{(1.24s^2 + 3.5s + 1)} \] \hspace{1cm} (2)

Level Control System:

\[ GP_{\text{level}}(s) = \frac{0.02 \exp(-5s)}{s(0.76s+1)} \] \hspace{1cm} (3)

3 Design of PID Controller

After deriving the transfer function model the controller has to be designed for maintaining the system to the optimal set point. This can be achieved by properly selecting the tuning parameters \(K_p, K_i\) and \(K_d\) for a PID Controller. The purpose of this paper is to investigate an optimal controller design using the evolutionary Programming, Genetic Algorithm, Particle Swarm Optimization and Bacterial foraging optimization. The initial values of PID gain are calculated using conventional Z – N method. Being hybrid approach, optimum value of gain is obtained using heuristic algorithm. The advantages of using heuristic techniques for PID are listed below. Heuristic Techniques can be applied for higher order systems without model reduction [5][6].These methods can also optimize the design criteria such as gain margin, Phase margin, Closed loop band width when the system is subjected to step & load change [5].Heuristic techniques like Genetic Algorithm, Evolutionary Programming, Particle Swarm Optimization and Bacterial foraging
Optimization methods have proved their excellence in giving better results by improving the steady state characteristics and performance indices.

### 3.1 GA based tuning of the controller

The optimal value of the PID controller parameters $K_p$, $K_i$, $K_d$ is to be found using GA. All possible sets of controller parameters values are particles whose values are adjusted to minimize the objective function, which in this case is the error criterion, and it is discussed in detail. For the PID controller design, it is ensured the controller settings estimated results in a stable closed-loop system [1]. This is the most challenging part of creating a genetic algorithm is writing the objective function. In this project, the objective function is required to evaluate the best PID controller for the system. An objective function could be created to find a PID controller that gives the smallest overshoot, fastest rise time or quickest settling time. However in order to combine all of these objectives it was decided to design an objective function that will minimize the performance indices of the controlled system instead [2]. Each chromosome in the population is passed into the objective function one at a time. The chromosome is then evaluated and assigned a number to represent its fitness, the bigger its number the better its fitness [6]. The genetic algorithm uses the chromosomes fitness value to create a new population consisting of the fittest members. Each chromosome consists of three separate strings constituting a P, I and D term, as defined by the 3-row bounds declaration when creating the population [3]. When the chromosome enters the evaluation function, it is split up into its three Terms. The newly formed PID controller is placed in a unity feedback loop with the system transfer function. This will result in a reduction in compilation time of the program. The system transfer function is defined in another file and imported as a global variable. The controlled system is then given a step input and the error is assessed using an error performance criterion such as Integral square error or in short ISE.

\[
ISE = \int_{0}^{\infty} e^2(t) dt
\]
The chromosome is assigned an overall fitness value according to the magnitude of the error, smaller the error larger the fitness value. Initializing the values of the parameters is as per Table 1. The flowchart of the GA control system is shown in figure 2.

![Flow Chart of GA](image)

**Fig.2.** Flow Chart of GA.

### 3.2 EP based tuning of the controller

There are two important ways in which EP differs from GA. First there is no constraint on the representation. The typical GA approach involves encoding the problem solutions as a string of representative tokens, the genome. In EP, the representation follows from the problem. A neural network can be represented in the same manner as it is implemented. For example, the mutation operation does not demand a linear encoding [5].

Second, the mutation operation simply changes aspects of the solution according to a statistical distribution which weights minor variations in the behavior of the offspring as highly probable and substantial variations as increasingly unlikely. The
The steps involved in creating and implementing evolutionary programming are as follows:

1. Generate an initial, random population of individuals for a fixed size (according to conventional methods $K_p$, $K_i$, $K_d$ ranges declared).

2. Evaluate their fitness (to minimize integral square error). $ISE = \int_0^\infty e^2(t)dt$

3. Select the fittest members of the population.

4. Execute mutation operation with low probability.

5. Select the best chromosome using competition and selection.

6. If the termination criteria reached (fitness function) then the process ends. If the termination criteria is not reached, then search for another best chromosome.

The EP parameters chosen are given in Table 1. The flowchart of the EP control system is shown in figure 3.

---

**Fig.3. Flow Chart of EP**
3.3 PSO based tuning of controller

The algorithm proposed by Eberhart and kennedy uses a 1-D approach for searching within the solution space. For this study the PSO algorithm will be applied to a 2-D or 3-D solution space in search of optimal tuning parameters for PI, PD and PID control. The flowchart of the PSO – PID control system [9] is shown in fig 5. Consider position $X_{i,m}$ of the $i^{th}$ particle as it traverses a $n$-dimensional search space: The previous best position for this $i^{th}$ particle is recorded and represented as $P_{best_{i,n}}$. The best performing particle among the swarm population is denoted as $gbest_{,n}$ and the velocity of each particle within the n-dimension is represented as $V_{i,n}$. The new velocity and position for each particle can be calculated from its current velocity and distance respectively [9]. So far (Pbest) and the position in the d-dimensional space [9]. The velocity of each particle is adjusted accordingly to its own flying experience and the other particles flying experience [14].

For example, the $i^{th}$ particle is represented, as $x_i=(x_{i,1}, x_{i,2}......x_{i,d})$ in the d-dimensional space. The best previous position of the $i^{th}$ particle is recorded as,

$\text{Pbest}_i = (\text{Pbest}_{i,1}, \text{Pbest}_{i,2}, \ldots, \text{Pbest}_{i,d})$ \hfill (4)

The index of best particle among all of the particles in the group in $gbest_{,d}$. The velocity for particle $i$ is represented as

$V_i = (V_{i,1}, V_{i,2}, \ldots, V_{i,d})$ \hfill (5)

The modified velocity and position of each particle can be calculated using the current velocity and distance from $P_{best_{i,d}}$ to $gbest_{,d}$ as shown in the following formulas

$$V_{i,m}^{(t+1)} = W V_{i,m}^{(t)} + c_1 \times \text{rand} \times (\text{Pbest}_{i,m} - x_{i,m}^{(t)})$$
$$+ c_2 \times \text{rand} \times (gbest_m - x_{i,m}^{(t)})$$ \hfill (6)

$$x_{i,m}^{(t+1)} = x_{i,m}^{(t)} + V_{i,m}^{(t+1)} \quad i=1,2,\ldots,n$$ \hfill (7)

Where $n$ is the number of particles in the group, $t = \text{Pointer of iterations (generations)}$, $V_{i,m}^{(t)} = \text{Velocity of particle \(i\) at iteration \(t\)}$, $W$ is the inertia weight factor, $c_1, c_2$ are the acceleration constants,
rand ()=Random number between 0 and 1, \( x_{i,m}^{(t)} \) is the current position of particle \( i \) at iteration \( t \), \( P_{best,i} \) is the best previous position of the \( i^{th} \) particle and \( g_{best,m} \) is the best particle among all the particles in the population. In the proposed PSO method each particle contains three members P, I and D. It means that the search space has three dimension and particles must ‘fly’ in a three dimensional space [9]. Initializing the values of the parameters is as per Table 1. The flow chart of PSO control system is shown in Figure 4.

Fig 4. Flowchart of PSO

3.4 Bacterial Foraging Optimization

The survival of species in any natural evolutionary process depends upon their fitness criteria, which relies upon their food searching and motile behavior. The law of evolution supports those species who have better food searching ability and either eliminates or reshapes those with poor search ability. The genes of those species who are stronger gets propagated in the evolution chain since they posses
ability to reproduce even better species in future generations. So a clear understanding and modeling of foraging behavior in any of the evolutionary species, leads to its application in any nonlinear system optimization algorithm. The foraging strategy of Escherichia coli bacteria present in human intestine can be explained by four processes, namely chemotaxis, swarming, reproduction, and elimination dispersal [7].

A. Chemotaxis

The characteristics of movement of bacteria in search of food can be defined in two ways, i.e. swimming and tumbling together known as chemotaxis. A bacterium is said to be ‘swimming’ if it moves in a predefined direction, and ‘tumbling’ if moving in a random direction. Mathematically, tumble of any bacterium can be represented by a unit length of random direction φ (j) multiplied by step length of that bacterium C(i). In case of swimming, this random length is predefined.

B. Swarming

For the bacteria to reach at the richest food location, it is desired that the optimum bacterium till a point of time in the search period should try to attract other bacteria so that together they conquer the desired location more rapidly. To achieve this, a penalty function based upon the relative distances of each bacterium from the fittest bacterium till that search duration, is added to the original cost function. Finally, when all the bacteria have merged into the solution point, this penalty function becomes zero. The effect of swarming is to make the bacteria congregate into groups and move as concentric patterns with high bacterial density.

C. Reproduction

The original set of bacteria, after getting evolved through several chemotaxis stages reaches the reproduction stage. Here, best set of bacteria gets divided into two groups. The healthier half replaces with the other half of bacteria, which gets eliminated, owing to their poorer foraging abilities. This makes the population of bacteria constant in the evolution process [11].

D. Elimination and dispersal

In the evolution process, a sudden unforeseen event can occur, which may
drastically alter the smooth process of evolution and cause the elimination of the set of bacteria and/or disperse them to a new environment. Most ironically, instead of disturbing the usual chemo tactic growth of the set of bacteria, this unknown event may place a newer set of bacteria nearer to the food location. From a broad perspective, elimination, and dispersal are parts of the population level long distance motile behavior. In its application to optimization, it helps in reducing the behavior of stagnation often seen in such parallel search algorithms. The flow chart of BFO control system is shown in Fig. 5.
4 Results and Discussion

A transfer function to validate the process is obtained with the real time data using Matlab system identification toolbox in equation (1.1-1.3).

Pressure Control System:

\[
GP_{pressure}(s) = \frac{0.62\exp(-0.15s)}{(0.5s+1)} \quad \text{------- (1)}
\]

Flow Control System:

\[
GP_{flow}(s) = \frac{0.5\exp(-6.5s)}{(1.24s^2 + 3.5s + 1)} \quad \text{------- (2)}
\]

Level Control System:

\[
GP_{level}(s) = \frac{0.02\exp(-5s)}{s(0.76s+1)} \quad \text{------- (3)}
\]

The tuned values through the traditional, as well as the proposed techniques, are analyzed for their responses to a unit step input, with the help of Matlab simulation. A tabulation of the time domain specifications comparison and the performance index comparison for the obtained models with the designed controllers is presented. The classical methods such as Ziegler Nichol method is employed to find out the values of \(K_p\), \(K_i\) and \(K_d\). Although the classical methods cannot be able to provide the best solution, they give the initial values or boundary values needed to start the soft computing algorithms. Due to the high potential of heuristic techniques such as EP, GA, PSO, BFO methods in finding the optimal solutions, the best values of \(K_p\), \(K_i\) and \(K_d\) are obtained. The simulations are carried out using INTEL[R], Pentium [R] CPU 2 GHZ, 1GB RAM in MATLAB 8.0 environment.

The Ziegler-Nichols tuning method using root locus and continuous cycling method were used to evaluate the PID gains for the system, using the “rlocfind” command in Matlab, the cross over point and gain of the system were found respectively.
Conventional methods of controller tuning lead to a large settling time, overshoot, rise time and steady state error of the controlled system. Hence Soft computing techniques is introduces into the control loop. GA, EP, PSO and BFO based tuning methods have proved their performance in giving better results by improving the steady state characteristics and performance indices. Performance characteristics of process were indicated and compared with the intelligent tuning methods as shown in the figure.6, figure.7 and figure.8 and values are tabulated in table 1, table.2, and table.3.

4.1 Simulation results for Pressure Control System:

Consider Equ. (1)

$$GP_{pressure}(s) = \frac{0.62e^{-0.15s}}{(0.5s+1)}$$

<table>
<thead>
<tr>
<th>Tuning Method</th>
<th>PID Parameters</th>
<th>Dynamic performance specifications</th>
<th>Performance Index</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$K_p$</td>
<td>$K_i$</td>
<td>$T_r$</td>
</tr>
<tr>
<td></td>
<td>(Proportional gain)</td>
<td>(Integral gain)</td>
<td>(Rise time)</td>
</tr>
<tr>
<td>ZN</td>
<td>3</td>
<td>6</td>
<td>3.66</td>
</tr>
<tr>
<td>EP</td>
<td>5</td>
<td>40</td>
<td>0.456</td>
</tr>
<tr>
<td>GA</td>
<td>2.4658</td>
<td>4.97</td>
<td>0.971</td>
</tr>
<tr>
<td>PSO</td>
<td>0.5190</td>
<td>0.9531</td>
<td>0.325</td>
</tr>
<tr>
<td>BFO</td>
<td>1.2989</td>
<td>2.8817</td>
<td>0.156</td>
</tr>
</tbody>
</table>

TABLE 1. Comparison result of Z-N and Heuristic methods—Pressure System.
From Table 1, the BFO tuned system displays a better performance than the PSO, GA, EP and ZN by achieving an ISE of 0.111. The closed-loop step response for the different tuning methods is illustrated in Figure 6. The response specifications and performance index for the pressure control loop are given in Table 1. From Figure 6 and Table 1, the PSO, GA and EP method yields a system with no overshoot, smaller settling and rise time in comparison to ZN method. The closed-loop response for the Z-N method yields higher overshoot and longer settling time. The BFO method delivers superior control performance with improved dynamic performance specifications over the other tuning methods.

![Fig 6](image)

**Fig.6.** Comparison result of Z-N and Heuristic methods-Pressure System

### 4.2 Simulation results for Flow Control System:

Consider the Equ. (2)

$$GP_{flow}(s) = \frac{0.5 \exp(-6.5s)}{1.24s^2 + 3.5s + 1}$$
From Table 2, the BFO tuned system displays a better performance than the PSO, GA, EP and ZN by achieving a ISE of $2.2236 \times 10^{-5}$. The closed-loop step response for the different tuning methods is illustrated in Figure 7. The response specifications and performance index for the pressure control loop are given in Table 2. From Figure 7 and Table 2, the PSO, GA and EP method yields a system with marginally higher overshoot, longer settling and rise time in comparison to BFO method. The closed-loop response for the Z-N method yields higher overshoot and longer settling time. The BFO method delivers superior control performance with improved dynamic performance specifications over the other tuning methods.

**TABLE 2.** Comparison result of Z-N and Heuristic methods - Flow system

<table>
<thead>
<tr>
<th>Tuning Method</th>
<th>PID Parameters</th>
<th>Dynamic performance specifications</th>
<th>Performance Index</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$K_p$ (Proportional gain)</td>
<td>$K_i$ (Integral gain)</td>
<td>$T_r$ (Rise time)</td>
</tr>
<tr>
<td>ZN</td>
<td>0.6</td>
<td>0.25</td>
<td>9.6</td>
</tr>
<tr>
<td>EP</td>
<td>0.456</td>
<td>0.12</td>
<td>19.1</td>
</tr>
<tr>
<td>GA</td>
<td>0.4</td>
<td>0.123</td>
<td>17.7</td>
</tr>
<tr>
<td>PSO</td>
<td>0.6</td>
<td>0.17</td>
<td>10</td>
</tr>
<tr>
<td>BFO</td>
<td>0.7</td>
<td>0.1689</td>
<td>9.6</td>
</tr>
</tbody>
</table>
4.3 **Simulation results for Level Control System:**

Consider the Equ. (3)

\[ GP_{level}(s) = \frac{0.02 \exp(-5S)}{s(0.76S+1)} \]
TABLE 3. Comparison result of Z-N and Heuristic methods-Level System

<table>
<thead>
<tr>
<th>Tuning Method</th>
<th>PID Parameters</th>
<th>Dynamic performance specifications</th>
<th>Performance Index</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$K_p$ (Proportional gain)</td>
<td>$K_i$ (Integral gain)</td>
<td>$T_r$ (Rise time)</td>
</tr>
<tr>
<td>ZN</td>
<td>5.5</td>
<td>0.5</td>
<td>2.37</td>
</tr>
<tr>
<td>EP</td>
<td>18.5</td>
<td>0.7</td>
<td>17.4</td>
</tr>
<tr>
<td>GA</td>
<td>7</td>
<td>0.0168</td>
<td>12.5</td>
</tr>
<tr>
<td>PSO</td>
<td>4</td>
<td>0.003</td>
<td>0.56</td>
</tr>
<tr>
<td>BFO</td>
<td>4.8</td>
<td>0.009</td>
<td>0.32</td>
</tr>
</tbody>
</table>

The closed-loop step responses of the PI controller tuned using the selected tuning methods are illustrated in Figure 8. The response specifications and performance index is given in Table 3. From Figure 8 and Table 3, the Z-N tuned response converges towards the stable region with unacceptable oscillation around the set point and larger overshoot. The other soft computing method produces a slower response with smaller overshoot than the BFO tuned response. The BFO tuned system results in quicker settling time and smaller overshoot when compared to the Z-N and other soft computing tuning methods.
5 Conclusion

The ZN, GA, EP, PSO, and BFO tuning methods have been implemented on pressure, flow and level control loops and a comparison of control performance using these methods has been completed. For the Z-N controller set point tracking performance is characterized by lack of smooth transition as well it has more oscillations. Also it takes much time to reach set point. The Soft computing based controller tracks the set point faster and maintains steady state. It was found for all control loops the performance of the Soft computing based controller was much superior to the Z-N control. Soft computing techniques are often criticized for two reasons: Algorithms are computationally heavy and convergence to the optimal solution cannot be guaranteed. PID controller tuning is a small-scale problem and thus computational complexity is not really an issue here. It took only a couple of seconds to solve the problem. Compared to conventionally tuned system, BFO tuned system has good steady state response and performance indices.
References


